
Interoperable Petri net models via ontology

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Abstract: The paper presents a Petri net infrastructure that should allow sharing Petri nets on the Semantic Web. Previous solutions only provide model interchange mechanisms between Petri net tools. The Petri net ontology is a central part of our solution. The ontology is closely related to the Petri Net Markup Language (PNML) – an ongoing Petri net community sharing effort. We developed the Petri net ontology using both UML and the Protégé tool, whereas we use RDF and OWL to represent the ontology. We implemented a Petri net software tool – P3 – that can be used to convert the Petri net ontology compliant models to the formats of current Petri net tools (*e.g.*, DaNAMiCS, Petri Net Kernel, PIPE) using eXtensible Stylesheet Language Transformations (XSLT). In order to show how the ontology can be used, we developed a simple educational web application that uses RDF-annotated ontology-based Petri net learning materials.

Keywords: Petri nets; interoperability; ontology development; Semantic Web; eXtensible Stylesheet Language Transformations (XSLT); OWL.

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1 Introduction

The main idea of this paper is to propose a suitable approach to Petri net (Peterson, 1981) applications on the Semantic Web, *i.e.*, an approach that would enable full semantic interoperability of Petri net models. Currently, Petri net interoperability is possible at the syntax level. Syntax level interoperability was first introduced by Berthelot *et al.* (1988), who pointed out that it would be very useful if Petri net researchers could share their Petri net model descriptions, so that more software tools could analyse the same model. So far, all Petri net interchange attempts have been mainly tool-specific, with very low (or without any) general acceptance. The Petri Net Markup Language (PNML) (Billington *et al.*, 2003) is a recent Petri net community effort that tries to provide XML-based model sharing. PNML tends to be a part of the future ISO/IEC High-level Petri net standard (ISO/IEC/JTC1/SC7 Working Group 19, 2002; Kindler, 2004). A particularly important advantage of this approach is that XML documents can be easily transformed using eXtensible Stylesheet Language Transformations (XSLT) into other formats (that need not necessarily be XML-based).

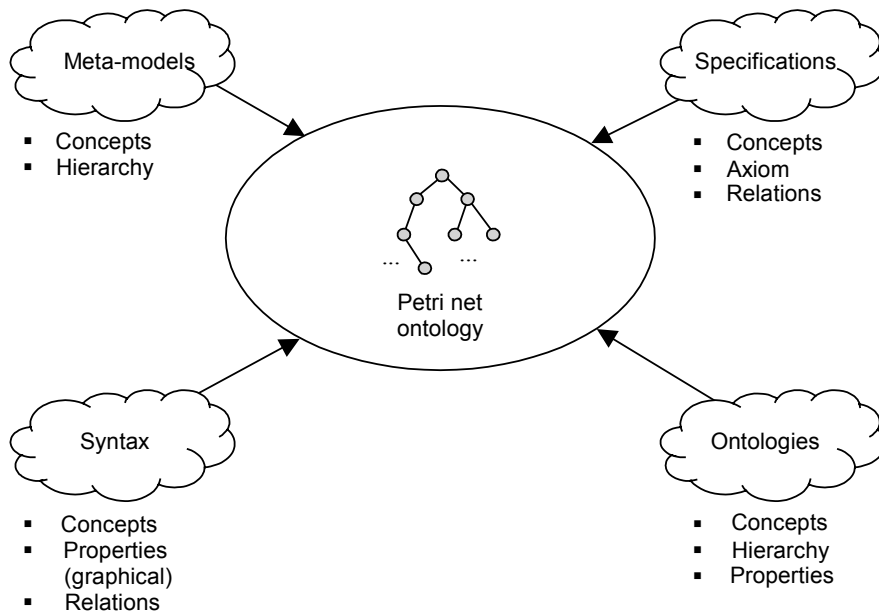
A suitable way to represent Petri nets is needed in order to reuse them more effectively on the Semantic Web. It requires defining the *Petri net ontology* for semantic description of Petri net concepts and their relationships. The Petri net ontology enables describing a Petri net using Semantic Web languages (*e.g.*, RDFS, and OWL) (Bechhofer *et al.*, 2004; Gómez-Pérez and Corcho, 2002). Petri nets described that way can be inserted into other, non-Petri net XML-based formats, such as *Scalable Vector Graphics* (SVG, the XML-based WWW Consortium (W3C) standard for 2D vector graphics) (Jackson, 2003), which makes possible the reconstruction of Petri net models using meta-data and annotations according to the Petri net ontology. We defined the Petri net ontology using experiences from previous Petri net formal descriptions (meta-model, ontologies and syntax). They indicate very useful directions for selecting key Petri net concepts and specifying their mutual relations. The PNML is of primary importance here – it is closely related to the Petri net ontology. Actually, it is a medium (syntax) for semantics. We additionally empowered the PNML usability by defining mappings to/from the Semantic Web languages (*i.e.*, RDFS and OWL).

The next section describes the main sources for defining Petri net ontology. We concentrate on Petri net syntax because most work has been done in solving this problem (we specifically discuss the PNML). Section 3 enumerates the advantages of the Petri net ontology, and gives guidelines for its construction. Section 4 outlines the development of the Petri net ontology – its initial design and implementation using UML and Protégé (Noy *et al.*, 2001) (*i.e.*, RDF Schema (RDFS)-based implementation), whereas Section 5 extends the ontology using an OWL-based UML profile in order to support the diversity of Petri net dialects. In Section 6, we present the tool we implemented to support the Petri net ontology, as well as an ontology-driven infrastructure for sharing Petri nets using PNML, XSLT and RDF.

2 Sources for Petri net ontology

This section analyses present Petri net specifications, meta-models, ontologies and syntax. Our main goal is to identify how each of these formal Petri net definitions can contribute to Petri net ontology. In Figure 1, we show the relations between the Petri net ontology we are developing and existing Petri net definitions. Also, this figure shows what we can use from all these sources to define the ontology.

Figure 1 Petri net ontology and elements that can be used from present formal ways for representing Petri nets



2.1 Specifications

We assume formal mathematical definitions as well as Petri net standards as Petri net specifications. Currently, there are many Petri net mathematical definitions for different Petri net dialects (Murata, 1989; Peterson, 1981). On the other hand, there is an initiative to adopt ISO/IEC High-level Petri net standard (ISO/IEC/JTC1/SC7 Working Group 19, 2002). We believe that from specifications, we can obtain concepts of Petri net domain, axioms, and relations between Petri net concepts.

2.2 Meta-models

Some authors believe that meta-model is closely related to ontology. Accordingly, an illustrative and very comprehensive Petri net meta-model is proposed by Breton and Bézivin (2001). Their starting point is that a meta-model defines a set of concepts and relations, *i.e.*, the terminology and a set of additional constraints (assertions). Note that this proposal is very important for the development of Petri net tools. However, it does not show how Petri nets can be used on the Semantic Web with non-Petri net tool (*i.e.*, annotation), and hence, how Petri nets are mapped into Semantic Web language (*e.g.*, RDF(S)). On the other hand, we can obtain useful guidelines on how to develop taxonomy (hierarchy) of Petri net concepts. Defining a Petri net UML profile produces a solution similar to the meta-model-based one, because UML profiles extend the UML meta-model by introducing stereotypes, tagged values and constraints. Hansen (2001) proposes a Petri net UML profile. Although this solution is meta-model-based, it is fairly awkward since it is based on the UML meta-model. This means that all UML concepts are introduced in the Petri net meta-model, but most of them are needless for the Petri net semantics. Also, this approach has the same limitation as the previous one in terms of support for Petri net dialects, Semantic Web use, and Petri net structuring mechanisms such as both pages and modules.

2.3 Ontologies

So far, only one Petri net ontology has been developed. Peleg and her colleagues developed a Petri net ontology using Protégé and a specific Graphical User Interface (GUI) that extends the standard GUI of the Protégé tool (Peleg *et al.*, 2002). Actually, this GUI provides graphical tools for all Petri net concepts (Places, Transitions and Arcs). In addition, the Petri net ontology is represented in RDFS, and concrete Petri net models are represented in RDF. This solution gives a solid starting point for defining the Petri net ontology. However, it has serious limitations. It covers only Time Petri nets, and no other kinds of Petri nets. It neither defines the Petri net structuring mechanisms, nor provides precise constraints (*e.g.*, types of an arc's source and target nodes that can be done using Protégé Axiom Language (PAL) constraints). Finally, it does not enable using other ontology languages for representing the Petri net ontology (*e.g.*, DAML or OWL). This ontology can give us guidelines on how to define conceptualisation, properties and taxonomy of the Petri net ontology.

2.4 Syntax

A lot of work has been done in defining and using Petri net syntax. We can classify present syntax in categories as follows: general-purpose and tool-specific. Tool-specific syntax are, for example, those that are used in the following tools: DaNAMiCS (regular text syntax) and Renew (XML). Abstract Petri Net Notation (APNN) is the first attempt to define a general-purpose Petri net syntax (*i.e.*, it has the ability to describe different Petri net dialects) (Bause *et al.*, 1995). The abstract notation for each Petri net class is defined in BNF. This grammar is useful from the extensibility and modularity perspectives. The Petri net community is working for three years already on the development of the Petri Net Markup Language (PNML) (Weber and Kindler, 2003) that might become a part of the future ISO/IEC High-level Petri net standard (ISO/IEC/JTC1/SC7 Working Group 19, 2002; Kindler, 2004). The PNML is a proposal that is based on XML. PNML specification is based on the PNML meta-model that formulates the structure of PNML documents. Actually, this meta-model defines the basic Petri net concepts (places, transitions, arcs), as well as their relations that can be presented in a PNML document. PNML, being more mature, is currently supported (or will be supported soon) by many Petri net software tools, for instance: Petri Net Kernel (PNK), CPN Tools, Worflan, PIPE, PEP, VIPTool, *etc.* For educational purposes, we developed *P3*, a Petri net tool that supports PNML (Gašević and Devedžić, 2004) (see Section 6 for details). We believe that the Petri net syntax mainly contributes to the Petri net ontology with: concepts, properties and their relations.

3 The Petri net ontology guidelines

As we have seen so far, Petri net formats use different concepts for defining their syntaxes. Some of these syntax-based approaches actually have problems with syntax validation. For instance, it is very difficult to validate a text-based document (*i.e.*, DaNAMiCS) without a special-purpose software for checking the corresponding format. A slightly better solution is to use DTD for XML definition as the Renew does. But, DTD does not support inheritance, does not have datatype checking (for the primary semantics checking), does not support defining specific formats, and moreover, a DTD document has non-XML structure. The W3C XML Schema overcomes most of DTD's problems. However, XML Schema has no full support for describing semantics (Klein, 2001). In fact, XML Schema is only a way for defining syntax. Furthermore, if we want to share Petri net models not only with Petri net tools on the Semantic Web, we must have a formal way of representing Petri net semantics since we cannot expect a non-Petri net tool to perform semantic validation.

We believe that the concept of ontology can be used for a formal description of Petri net semantics. In this paper, domain ontology is understood as a formal way for representing shared conceptualisation in some domain (Gruber, 1993). Ontology has formal mechanisms to represent concepts, concept properties and relations between concepts in the domain of discourse. With the Petri net ontology, we can overcome validation problems that we have already been noticed. However, the Petri net ontology does not exclude current Petri net formats (especially PNML). Ontology has relations to syntax, in the sense that syntax should enable ontological knowledge-sharing (Chandrasekaran *et al.*, 1999). With the Petri net ontology, we can use ontology

development tools for the validation of Petri net models (*e.g.*, Protégé). Also, having the Petri net ontology, one can use Semantic Web languages for representing Petri net models (*e.g.*, RDF, RDF Schema – RDF, DAML+OIL, OWL, *etc.*) (Gómez-Pérez and Corcho, 2002). Thus, we show how PNML can be used as a guideline for the Petri net ontology.

Accordingly, we think that Petri net ontology should have a common part that contains concepts common to all Petri net dialects. Afterwards, this common part will be specialised for concrete Petri net dialects. Actually, this is the same principle that uses PNML (Billington *et al.*, 2003). In Figure 2, we show a common part of Petri net ontology that we call Core Petri net ontology. The Core Petri net ontology is extracted from the analysed ontology sources.

Figure 2 Conceptualisation of the Core Petri net ontology: key concepts, their mutual relations, and cardinality

<p>Net</p> <ul style="list-style-type: none"> ▪ place (0..*) ▪ transition (0..*) ▪ page (0..*) ▪ place reference (0..*) ▪ transition reference (0..*) ▪ module instance (0..*) <p>Place</p> <ul style="list-style-type: none"> ▪ name (1) ▪ marking (1) ▪ initial marking (1) ▪ position (1) <p>Transition</p> <ul style="list-style-type: none"> ▪ name (1) ▪ position (1) <p>Arc</p> <ul style="list-style-type: none"> ▪ from node (1) ▪ to node (1) ▪ position (0..*) ▪ multiplicity (1) <p>Page</p> <ul style="list-style-type: none"> ▪ place (0..*) ▪ transition (0..*) ▪ page (0..*) ▪ place reference (0..*) ▪ transition reference (0..*) ▪ module instance (0..*) <p>Module</p> <ul style="list-style-type: none"> ▪ name (1) ▪ place (0..*) ▪ transition (0..*) ▪ arc (0..*) ▪ page (0..*) ▪ place reference (0..*) ▪ transition reference (0..*) ▪ module instance (0..*) ▪ module interface (1) 	<p>Module instance</p> <ul style="list-style-type: none"> ▪ name (1) ▪ place (0..*) ▪ transition (0..*) ▪ arc (0..*) ▪ page (0..*) ▪ place reference (0..*) ▪ transition reference (0..*) ▪ module instance (0..*) ▪ module interface (1) <p>Module interface</p> <ul style="list-style-type: none"> ▪ input (0..*) ▪ output (0..*) <p>Place reference</p> <ul style="list-style-type: none"> ▪ reference (1) ▪ name (1) ▪ position (1) <p>Transition reference</p> <ul style="list-style-type: none"> ▪ reference (1) ▪ name (1) ▪ position (1) <p>Graphical information</p> <ul style="list-style-type: none"> ▪ position (1) ▪ font style (1) ▪ colour (1) ▪ ... <p>Marking</p> <ul style="list-style-type: none"> ▪ token (0..*) ▪ graphical information (1) <p>Initial marking</p> <ul style="list-style-type: none"> ▪ token (0..*) ▪ graphical information (1) <p>Name</p> <ul style="list-style-type: none"> ▪ graphical information (1) <p>Token</p> <ul style="list-style-type: none"> – <p>Multiplicity</p> <ul style="list-style-type: none"> ▪ graphical information (1)
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We introduced some concepts that do not really exist in Petri net models in order to obtain more suitable concept hierarchy in the core ontology. We call these concepts synthetic concepts. Overview of these concepts is given in Table 1. The meanings of some of the Petri net concepts we refer to in the table (*e.g.*, module, structural element, *etc.*) are clarified in the next section. In the next section, we define the Petri net ontology using UML and Protégé ontology development tool.

Table 1 Overview of the synthetic concepts in the Core Petri net ontology – generalisations of concepts from Figure 2

<i>Synthetic concept</i>	<i>Generalise concepts</i>
Node reference	Place reference, transition reference
Node	Place, transition, node reference
Structural element	Page, module instance
Model element	Structural element, arc, node

4 The Petri net ontology – initial implementation

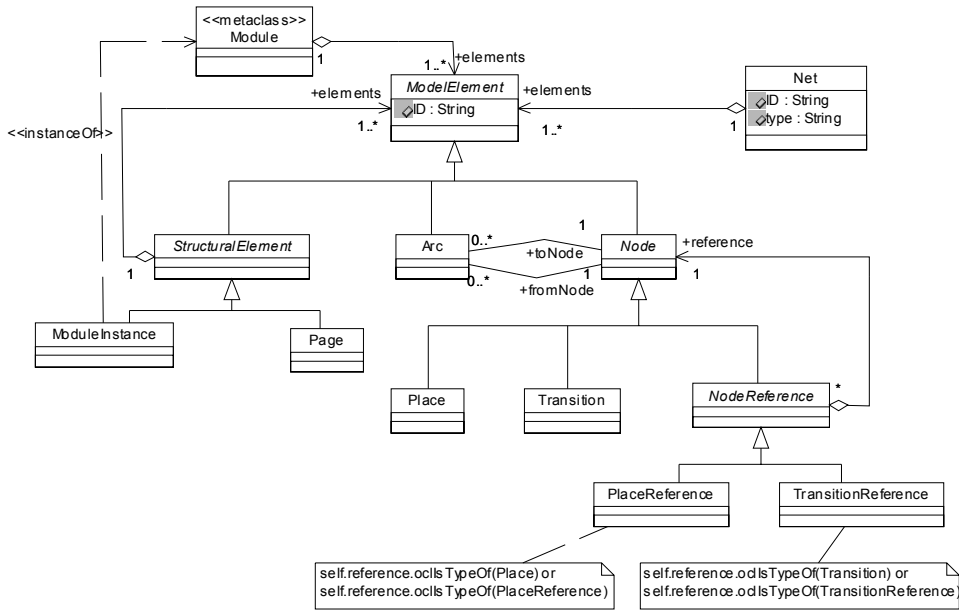
In order to develop the Petri net ontology, we decided to use UML (Kogut *et al.*, 2002). UML was suitable because it is a generally accepted and standardised tool for analysis and modelling in software engineering. We were also able to employ UML-based Petri net descriptions existing within the PNML definition (Billington *et al.*, 2003). However, neither the UML tools nor the UML itself is intended to be used for ontology development. Thus, in order to achieve more precise Petri net definitions than a UML model provides, it is necessary to use an ontology development tool. We decided to use Protégé 2000 (Noy *et al.*, 2001) since it is a popular tool for ontology development and can import UML models. This is enabled by Protégé's UML backend that imports UML models (represented in *XML Metadata Interchange (XMI)* format) into a Protégé ontology.

4.1 The conceptual solution: a UML model

The hierarchy of core concepts of the Petri net ontology is shown in Figure 3. In our design of the Petri net ontology, there is a single root element that we call *ModelElement*. This element is the parent of all elements of the Petri net structure. The name of this class is *ModelElement* because the UML meta-model uses the same name for its root class (OMG Document Formal/03-03-01, 2003). A Petri net (the *Net* class) can contain many different *ModelElements*. Since we regard that a *ModelElement* may belong to one and only one Petri net, we have a unidirectional association from *Net* to *ModelElement*. *ModelElement* and *Net* have the ID attribute (unique identifier) of String type, and *Net* also has an attribute that describes the type of the Petri net. It is in accordance with PNML. The three main Petri net concepts (place, transition and arc) define the structure of a Petri net, and they are represented in Figure 3 with the corresponding classes (*Place*, *Transition*, and *Arc*). Places and transitions are kinds of nodes (*Node*). In some Petri nets, an arc connects two nodes of different kinds. However, it is important to say that this is not a general Petri net ontology statement, since there are Petri net dialects where an arc

can connect, for instance, two transitions (Semenov *et al.*, 1997). Hence we did not include this statement in the core Petri net ontology, but it should be defined in ontology extensions for different Petri net dialects.

Figure 3 The Petri net ontology – hierarchy of core Petri net concepts



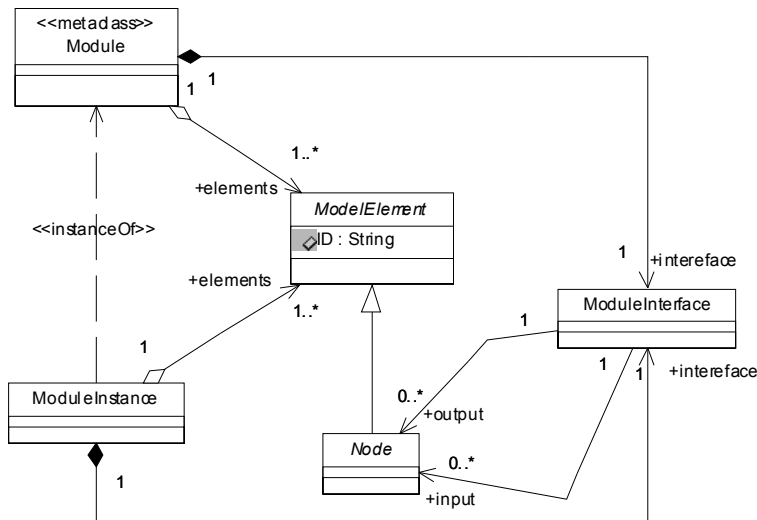
The *Node* class is introduced in the ontology in order to have a common way to reference both places and transitions. In order to make Petri net models easy to maintain, different concepts for structuring can be used. In the Petri net ontology, we have the class *StructuralElement*. This class is inherited from *ModelElement*, and we inherit from this class all classes that represent structuring mechanisms. Also, a *StructuralElement* may contain many *ModelElements*, but *ModelElements* do not need the information which *StructuralElement* they belong to (if any). Accordingly, we have unidirectional aggregation from *StructuralElement* to *ModelElement*. We have decided to support two common mechanisms: pages (the *Page* class), and modules (the *Module* meta-class). A *Page* may consist of other Petri net *ModelElements* – it may even consist of other *StructuralElements* (e.g., *Page* and *ModuleInstance*). A *NodeReference*, which can be either a *TransitionReference* or a *PlaceReference*, represents an appearance of a node. Since it is not important for a *Node* to know what *NodeReferences* refer to it, we have a unidirectional aggregation from *NodeReference* to *Node*. Here, there are also constraints: a *TransitionReference* can refer to either a *Transition* or another *TransitionReference*, while a *PlaceReference* can refer to either a *Place* or another *PlaceReference*. The *Decorator* design pattern (Gamma *et al.*, 1995) was used to represent referencing of a *NodeReference*. Of course, the pattern is not a part of the UML language, but it is a design matter. The reason we applied this design pattern is to have a more suitable model of Petri nets for some future implementations of the ontology. We show these constraints

using OCL in Figure 3. These constraints also affect the OCL constraint for arcs that we have already described. Unlike the OCL statement for arcs, this statement can be applied on all Petri net dialects (see the OCL constraints in Figure 3).

The second kind of structuring mechanisms are modules. A *Module* consists of *ModelElements* (even other *StructuralElements*, i.e., *Page* and *ModuleInstance*), and it can be instantiated (much like an object is instantiated from a class in the object-oriented paradigm). Accordingly, *Module* is a meta-class (the stereotype in Figure 3), and *ModuleInstance* depends on *Module* (that shows a stereotyped *instanceOf* dependency from *ModuleInstance* to *Module*). Figure 4 describes both *Module* and *ModuleInstance* classes in detail. One can see that these two classes also have one *interface*. Type of this *interface* is the *ModuleInterface* class that has two collections of *ModelElements*: output (a collection of output *Nodes*) and input (a collection of input *Nodes*). Note that these input and output *Nodes* can only be *Places* and *Transitions*, and this is expressed by the following OCL constraint:

```
context ModuleInterface:
  inv:
    (self.output.oclTypeOf(Place) or self.output.oclTypeOf(Transition)) and
    (self.input.oclTypeOf(Place) or self.input.oclTypeOf(Transition))
```

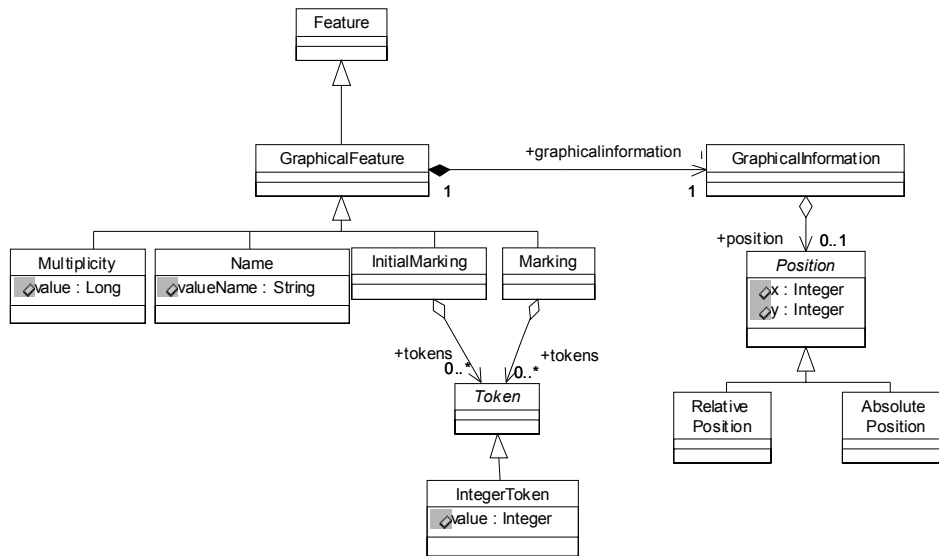
Figure 4 Both *Module* and *ModuleInstance* classes have interface that consists of *input* and *output Nodes*



In Petri nets, an additional property (or feature) can be attached to almost every core Petri net element (e.g., name, multiplicity, etc.). Thus, we have included in the Petri net ontology a description of features and in Figure 5 we shortly depict how these features have been added. All UML model elements shown in the figure belong to the core Petri net ontology. The root class for all features is *Feature*. This is also similar to the UML meta-model. The Petri net ontology follows the PNML’s classification of features: those that contain graphical information (annotation) and those that do not have them (attribute). In the Petri net ontology every feature directly inherited from *Feature* class is an attribute, whereas *GraphicalFeature* class represents annotations.

GraphicalFeature has graphical information that can consist of, for instance, position (the *Position* class and its children *Absolute Position* and *Relative Position*). Examples of graphical features are: *Multiplicity*, *Name*, *InitialMarking* and *Marking*. It is interesting to notice that marking and initial marking consist of tokens (the *Token* class). In order to support token colours, the *Token* class is abstract. In Figure 5 we show a case where there are no colours attached to tokens; instead, we just take into account the number of tokens (*IntegerToken*).

Figure 5 The property hierarchy of the Petri net ontology. The hierarchy is a part of the core Petri net ontology



Attaching a new feature to a Petri net class requires just adding an association between a class and a feature. A UML description is a convenient way of representing the Petri net semantics. Also, this Petri net ontology can be used as a Petri net meta-model in future Petri net implementations that can take advantage of the MDA concept and repository-based software development (Bock, 2003). However, it does not let us semantically validate Petri net models. For example, we cannot use OCL statements to perform this task. In addition, UML attributes and ontology properties are semantically different concepts. Unlike a UML's attribute, ontology property is a first-class concept that can exist independently of any ontology class (Baclawski *et al.*, 2002).

There are two ways to further refine the Petri net ontology. The first one is to use a UML profile (Kogut, 2002) for UML-based ontology development. The second one recommends using standard ontology development tools. We decided to use:

- 1 Protégé 2000, since it provides all the necessary ontology development features (constraints and support for ontology languages), but also has the ability to use the UML models we have shown.
- 2 The Ontology UML profile (Djurić *et al.*, 2005) that is based on OWL.

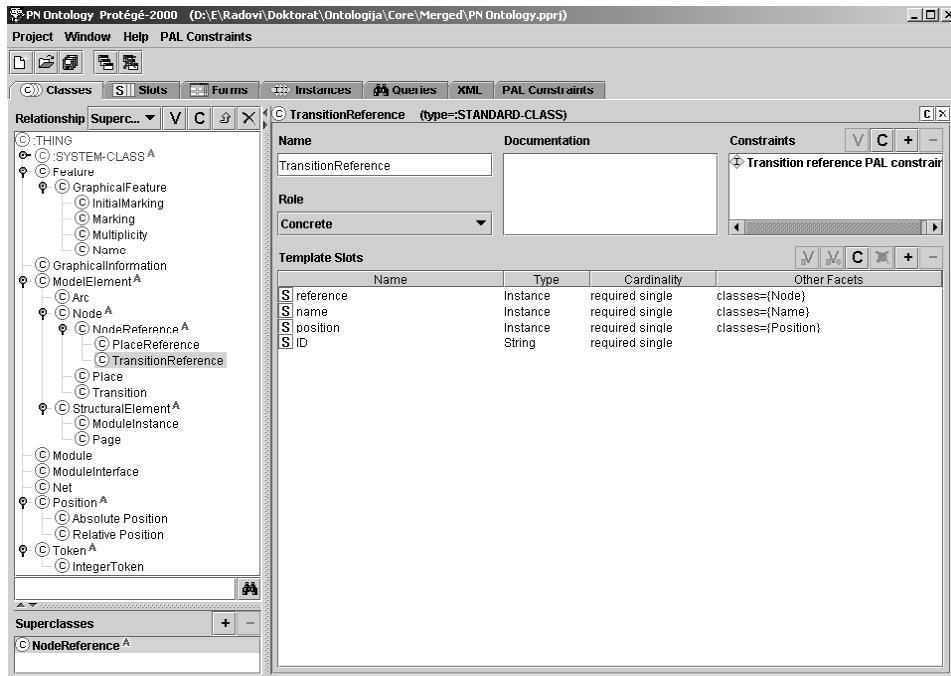
4.2 The Petri net ontology in the Protégé tool

We can precisely define the Petri net ontology in Protégé 2000. We can distinguish between a class and a meta-class (e.g., *Module* – a meta-class, *ModuleInstance* – a class), we can use different Semantic Web languages provided through Protégé's backends (RDF(S), OWL, DAML+OIL) to represent the Petri net ontology, and we can specify the constraints that we defined in the UML model using OCL (e.g., PAL). We can then validate all ontology instances using these constraints, and detect if there is any instance that does not conform to some of the constraints. For instance, here is the PAL constraint on the TransitionReference class, which is equivalent to the OCL constraint on the same class from Figure 3:

```
(defrange ?transitionRef :FRAME TransitionReference)
(forall ?transitionRef (or
  (instance-of (reference ?transitionRef) Transition)
  (instance-of (reference ?transitionRef) TransitionReference)))
```

After the initial UML design of the Petri net ontology, it was imported into the Protégé using Protégé's UML backend.¹ This plug-in has the ability to read an XML format (i.e., XMI) for representing UML models. The main shortcoming of this UML backend is that it is unable to map UML class associations. Thus we had to manually add all the slots that are represented in UML as association ends. A snapshot of the Petri net ontology after we imported it and inserted all slots (i.e., association ends) in Protégé is shown in Figure 6.

Figure 6 The Petri net ontology in Protégé 2000



Of course, Protégé does not have the ability to transform OCL constraints into PAL constraints. Thus we have also manually reconstructed all OCL-defined constraints from the UML model of the Petri net ontology into a set of corresponding PAL constraints.

Using Protégé, we generated the RDFS that describes the Petri net ontology. One can use it for reasoning about a document that contains a Petri net model. Figure 7 shows an excerpt of this RDFS. This figure depicts how RDFS defines the classes for *ModelElement*, *Node*, *Transition*, *Place*, *Arc*, and *ArcType*. Also, this figure shows how RDFS defines *Feature*, as well as how *name* feature is defined and attached to classes that should have this property.

Since Protégé supports more concepts for ontology definition than RDFS does, one can notice some extensions of RDFS in Figure 7. Note that this RDFS/XML syntax generated by Protégé relays on the old RDFS semantics for `rdf:domain` property where the multiple domain of the property is regarded as a union of all domain classes. According to the new RDFS semantics, if a property has more than one domain property, any resource that has that property is an instance of all of the classes specified as the domains (*i.e.*, intersection of domain classes). These Protégé extensions are manifested by namespace `a`. For example, they are used to define cardinality (`a:maxCardinality`, `a:minCardinality`), to refer to a PAL constraint (`a:slot_constraints`), *etc.* Of course, this is neither a limitation of the Petri net ontology nor of the Protégé tool, but of RDFS itself. Most of such limitations are overcome in the forthcoming OWL (Bechhofer *et al.*, 2004), but this discussion is beyond the scope of this paper.

Figure 7 A part of the RDF Schema of the Petri net ontology

```

<rdf:RDF xmlns:rdf="&rdf;" xmlns:a="&a;" xmlns:rdfs="&rdfs;">
  <!-- ... -->
  <rdfs:Class rdf:about="ModelElement" a:role="abstract"
    rdfs:label="ModelElement">
    <rdfs:subClassOf rdf:resource="&rdfs;Resource"/>
  </rdfs:Class>
  <rdfs:Class rdf:about="Node" a:role="abstract" rdfs:label="Node">
    <rdfs:subClassOf rdf:resource="ModelElement"/>
  </rdfs:Class>
  <rdfs:Class rdf:about="Place" rdfs:label="Place">
    <rdfs:subClassOf rdf:resource="Node"/>
  </rdfs:Class>
  <rdfs:Class rdf:about="PlaceReference" rdfs:label="PlaceReference">
    <rdfs:subClassOf rdf:resource="NodeReference"/>
    <a:_slot_constraints rdf:resource="PN Ontology_00023"/>
  </rdfs:Class>
  <rdfs:Class rdf:about="Feature" rdfs:label="Feature">
    <rdfs:subClassOf rdf:resource="&rdfs;Property"/>
  </rdfs:Class>
  <!-- ... -->
  <rdf:Property rdf:about="name" a:maxCardinality="1"
    a:minCardinality="1" rdfs:label="name">
    <rdfs:range rdf:resource="Name"/>
    <rdfs:domain rdf:resource="Node"/>
    <rdfs:domain rdf:resource="Place"/>
    <rdfs:domain rdf:resource="PlaceReference"/>
    <rdfs:domain rdf:resource="Transition"/>
    <rdfs:domain rdf:resource="TransitionReference"/>
  </rdf:Property>
  <!-- ... -->
</rdf:RDF>

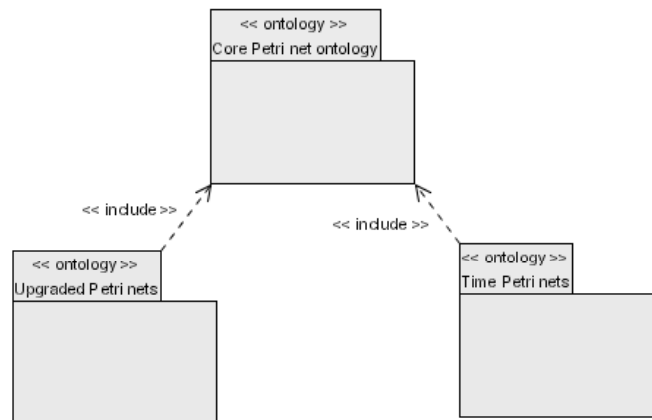
```

On the other hand, one can see that the RDFS/Protégé Petri net ontology does not take into account Petri net dialects. In this version of the Petri net ontology, we can add Petri net dialect-specific properties or constraints, but we have no ability to distinguish between the core concepts from the Petri net ontology and Petri net dialect-specific concepts. One possible solution is to use XML/RDF namespace mechanism. But, this solution is also limited for use in Protégé. We need a better way to represent ontology modularisation. Accordingly, we decided to use OWL and an OWL-based UML profile in order to overcome these RDF(S) limitations of the Petri net ontology.

5 OWL-based Petri net ontology

For ontology development, we use the Ontology UML profile (OUP) (see Djurić *et al.*, (2005) for details) that is based on the forthcoming ontology language OWL (Bechhofer *et al.*, 2004). The OUP provides stereotypes and tagged values for full ontology development. OUP models can be (automatically) transformed into OWL ontologies (*e.g.*, using XSLT) (Gašević *et al.*, 2005). Using the OUP, one can represent the relations between the core concepts of the Petri net ontology and the specifics of a Petri net dialect. For that purpose, we suggest using the OUP's package mechanism. In the OUP, we attach `<<ontology>>` to a package. That means the package is an ontology. Accordingly, we can put all core concepts of the Petri net ontology in an `<<ontology>>` package. If we extend the Petri net ontology with concepts of a Petri net dialect, we only need to create a new `<<ontology>>` that would be related with the core `<<ontology>>` through the `<<include>>` dependency. In Figure 8 we illustrate this extension principle.

Figure 8 Extension mechanism of the Petri net ontology: support for Petri net dialects



This example depicts how we extend the Core Petri net ontology (`<<ontology>>` *Petri net core*) with concepts of Upgraded and Time Petri nets (*e.g.*, we attach new properties to the core classes for a Petri net dialect). An additional advantage of this approach is that we have the ability to merge concepts from a number of ontologies (*i.e.*, `<<ontology>>` packages). As a result we obtain one ontology definition, for instance,

in OWL (by applying XSLT). Comparing with the current PNML proposal for the Petri Net Definition Types (Billington *et al.*, 2003), one can see that this approach improves the maintainability of Petri net concepts, and better supports reusability of the Petri net ontology concepts. So far, we have defined the Petri net ontology extensions for P/T nets, Time Petri nets and Upgraded Petri nets.

5.1 The Core Petri net ontology

The Core Petri net hierarchy, which is shown in Figure 3, is the same for the Petri net ontology represented in the OUP. Actually, there is a difference with regard to both associations and attributes in the model from Figure 3, since ontology development understands property as a first-class concept. Thus, it is necessary to transform all association between classes as well as all class attributes into the OUP property stereotypes (`<<DatatypeProperty>>` and `<<ObjectProperty>>`). Note that in the OUP Petri net ontology, we do not need the *Feature* class since property is the first class in ontology development. Accordingly, we have `<<ObjectProperty>>` and `<<DatatypeProperty>>` that represent properties in the Petri net ontology. On the other hand, we want to provide support for graphical features (*GraphicalFeature*). Figure 9 gives an example of the `<<ObjectProperty>>` *name* that has already been declared as a graphical feature. In this case, the *name* property has as its range (through the `<<range>>` association) the *NameDescriptor* `<<OntClass>>`. However, this class is inherited from the *GraphicalFeature*. *GraphicalFeature* is introduced in the Petri net ontology to be the root class for all the classes that constitute the range for a graphical feature. Similarly, we define other graphical features (e.g., marking). In addition, the *name* property has its domain (the `<<domain>>` association) in the union of the *Net* and *Node* classes.

Figure 9 An example of a graphical feature defined in the Ontology UML profile: name object property

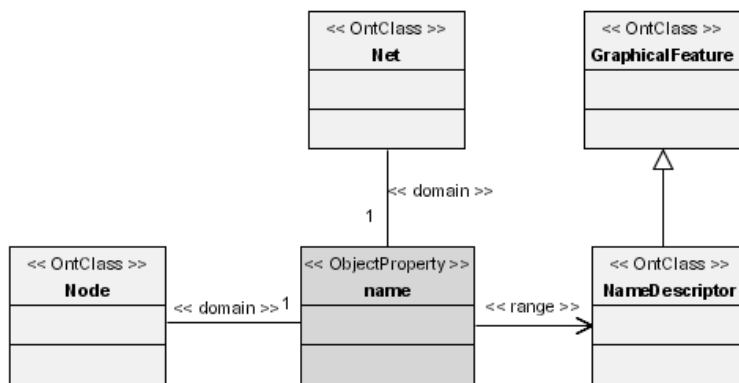


Figure 10 shows an excerpt of the Petri net ontology in OWL. It was generated using an XSLT for transformation from the OUP ontology (*i.e.*, XMI) to OWL (Gašević *et al.*, 2005). The figure illustrates a part of the OWL *TransitionReference* restriction on the

reference property. This restriction states that *TransitionReference*'s property *reference* must take all values from (*allValuesFrom*) the union of the following classes: *Transition* and *TransitionReference*. It is important to note that in the OWL ontology, logical expressions (*owl:unionOf*) take an XML form (e.g., the *TransitionReference* restriction), unlike the Protégé PAL constraints that are written in a Lisp-like form. It is more convenient to parse an ontology statement represented in an XML format using standard XML parser, as well as transform it using the XSLT mechanism.

Figure 10 A part of the Petri net ontology in OWL: the *TransitionReference* class restriction from Figure 3 expressed in OCL. This is also shown in PAL in Section 4.2

```

<owl:Class rdf:ID="TransitionReference">
  <rdfs:subClassOf rdf:resource="#NodeReference"/>
  <rdfs:subClassOf>
    <owl:Restriction>
      <owl:onProperty rdf:resource="#reference"/>
      <owl:allValuesFrom>
        <owl:Class>
          <owl:unionOf rdf:parseType="Collection">
            <owl:Class rdf:about="#Transition"/>
            <owl:Class rdf:about="#TransitionReference"/>
          </owl:unionOf>
        </owl:Class>
      </owl:allValuesFrom>
    </owl:Restriction>
  </rdfs:subClassOf>
</owl:Class>

```

5.2 An extension example: Upgraded Petri nets

Here we illustrate the ontology that describes Upgraded Petri nets (Štrbac, 2002) (a Petri net dialect for modelling hardware), in order to show how the Petri net ontology can be extended. The same procedure can be applied to describe other Petri net dialects (e.g., Time Petri nets, Coloured Petri nets, etc.). Figure 11 shows the concepts that should be introduced in the ontology in order to support Upgraded Petri nets. Most of these concepts are ontology properties: *attribute X*, *attribute Y* are graphical features of the Place class; *function*, *function firing level*, and *time function* are features of the Transition class; and *typeArc* is a feature of the Arc class. The ontology extension for Upgraded Petri nets also requires a restriction on the Arc class: an arc can only connect a place and a transition.

Figure 11 Relation between the Core Petri net concepts and their Upgraded Petri net extensions

Core ontology concepts	PLACE	TRANSITION	ARC
Upgraded Petri net extensions	<ul style="list-style-type: none"> ▪ <i>attribute X</i> – graphical feature ▪ <i>attribute Y</i> – graphical feature 	<ul style="list-style-type: none"> ▪ <i>function</i> – feature ▪ <i>function firing level</i> – feature ▪ <i>time function</i> – feature 	<ul style="list-style-type: none"> ▪ <i>an arc can only connect a place and a transition</i> – restriction ▪ <i>typeArc</i> – feature

In terms of OUP, this extension means that we have a new <<ontology>> package, which contains all Upgraded Petri net-specific concepts and restrictions. Figure 12 shows how we attached the *typeArc* property to the *Arc* class. In fact, the domain of the *typeArc* property is *Arc* whereas the enumeration *ArcType* is the range of the *typeArc*. The enumeration *ArcType* consists of four individuals: normal, inhibitor, reset and read.

Figure 12 An extension of the *Arc* class for the Upgraded Petri nets: the *typeArc* property with its range (enumeration of the following values – normal, inhibitor, reset and read)

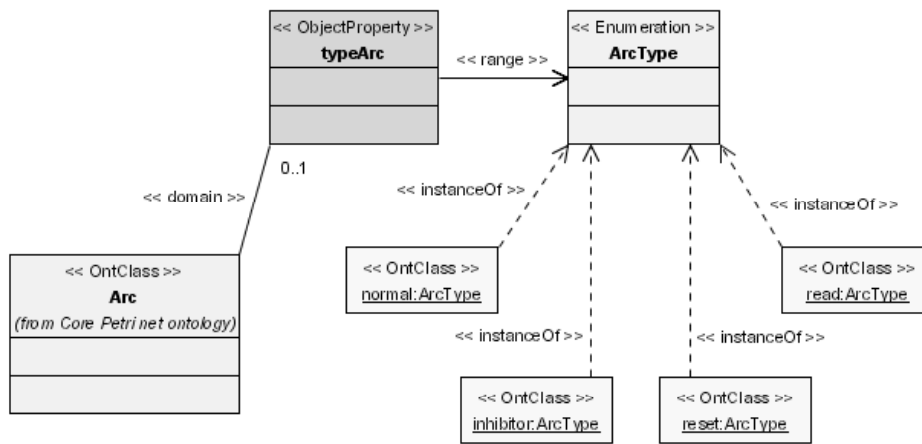


Figure 13 OWL definition of the *Arc* class: a) for the Core Petri net ontology; b) for the ontology of Upgraded Petri nets

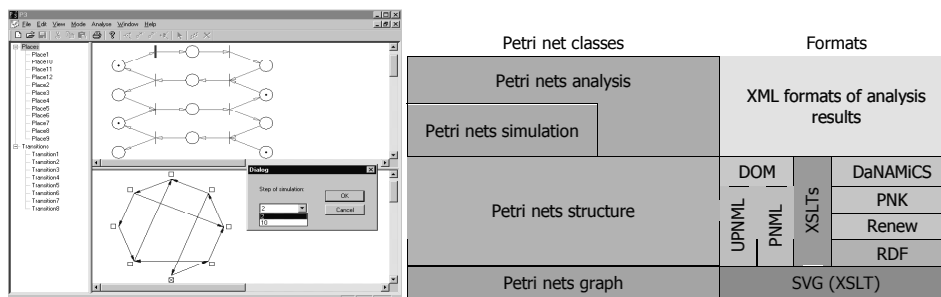
<pre> <owl:Class rdf:ID="Arc"> <rdfs:subClassOf rdf:resource="#ModelElement"/> <rdfs:subClassOf> <owl:Restriction> <owl:onProperty rdf:resource="#multiplicity"/> <owl:maxCardinality rdf:datatype="#xsd:nonNegativeInteger"> 1</owl:maxCardinality> </owl:Restriction> </rdfs:subClassOf> <rdfs:subClassOf> <owl:Restriction> <owl:onProperty rdf:resource="#fromNode"/> <owl:cardinality rdf:datatype="#xsd:nonNegativeInteger"> 1</owl:cardinality> </owl:Restriction> </rdfs:subClassOf> <rdfs:subClassOf> <owl:Restriction> <owl:onProperty rdf:resource="#toNode"/> <owl:cardinality rdf:datatype= "#xsd:nonNegativeInteger"> 1</owl:cardinality> </owl:Restriction> </rdfs:subClassOf> </owl:Class> </pre> <p style="text-align: center;">a)</p>	<pre> <owl:ObjectProperty rdf:ID="typeArc"> <rdfs:range rdf:resource="#ArcType"/> <rdfs:domain rdf:resource="#Arc"/> </owl:ObjectProperty> <owl:Class rdf:ID="ArcType"> <owl:oneOf rdf:parseType="Collection"> <ArcType rdf:about="#normal"/> <ArcType rdf:about="#inhibitor"/> <ArcType rdf:about="#reset"/> <ArcType rdf:about="#read"/> </owl:oneOf> </owl:Class> <ArcType rdf:ID="normal"/> <ArcType rdf:ID="inhibitor"/> <ArcType rdf:ID="reset"/> <ArcType rdf:ID="read"/> <owl:Class rdf:ID="Arc"> <!-- This extended Arc class has the same content as the Arc class in the Core Petri net ontology plus the following content: --> <rdfs:subClassOf> <owl:Restriction> <owl:onProperty rdf:resource="#typeArc"/> <owl:maxCardinality rdf:datatype="#xsd:nonNegativeInteger"> 1</owl:maxCardinality> </owl:Restriction> </rdfs:subClassOf> <!--Restriction that an arc can only connect a place and transition--> </owl:Class> </pre> <p style="text-align: center;">b)</p>
---	---

Having introduced all Upgraded Petri net concepts and restrictions in the OUP model, we can generate its OWL equivalent using XSLT (Gašević *et al.*, 2005). Figure 13 contains an excerpt of the generated OWL ontology for the *Arc* class. On the left side (Figure 13a) we give the *Arc* class definition of the Core Petri net ontology. On the right side (Figure 13b) we show an excerpt of the *Arc* class definition of the ontology for Upgraded Petri nets. It should be noted that Figure 13b only depicts how the *typeArc* property is added in the OWL ontology. Firstly, we added the *typeArc* property as a definition of a new object property, which has the *Arc* class as its domain, and the *ArcType* class as its range. *ArcType* is an enumeration that consists of the individuals we have already mentioned. The *Arc* class only has a cardinality restriction on the *typeArc* property. Note that the *Arc* class for Upgraded Petri nets contains all definition of the *Arc* class from the Core Petri net ontology (*i.e.*, from Figure 13a). Following the same principle, the XSLT converter produced the other parts of the OWL ontology for Upgraded Petri nets.

6 Tools for the Petri net ontology

In order to show practical tool support for the Petri net ontology, we depict the P3 tool. This tool has been initially developed for Petri net teaching (Gašević and Devedžić, 2004), but we extended it, and thus it can be used in conjunction with the Petri net ontology. Being based on the PNML concepts, P3 is compatible with PNML. The P3 tool supports P/T nets and Upgraded Petri nets. A P3 screenshot is shown in Figure 14a. The P3's architecture is shown in Figure 14b. P3's classes supporting different Petri net functionalities (Petri net classes) is shown on the left in Figure 14b, whereas the supported formats are on the right side.

Figure 14 P3, ontology-based Petri net tool: a) P3 screenshot; b) P3 architecture: classes supporting different Petri net functionalities (Petri net classes) and supported XML formats



The formats supported by P3 are the main point of interest for the Petri net ontology. The P3's model-sharing mechanism is based on using PNML. All other formats are implemented in P3 using XSLT (from the PNML). Accordingly, P3 can export to the following Petri net tool formats: *DaNAMiCS* – a tool that uses an ordinary text format; *Renew* – a tool that uses another XML-based format; *Petri Net Kernel* – a tool that uses PNML, but since there are some differences between this PNML application and the P3's PNML, we had to implement an XSLT; *PIPE* – a tool that uses PNML (no need for XSLT).

P3 tool has the ability to generate RDF description of a Petri net. This P3's feature is also implemented using XSLT. The generated RDF is in accordance with the Petri net ontology (in its RDFS form). We also implemented the XSLT for the opposite direction, *i.e.*, to transform RDF into PNML, and hence we can analyse RDF-defined Petri nets using standard Petri net tools. P3 implements conversion of the PNML Petri net model description to SVG. Since this format can be viewed in standard web browsers, it is suitable for creating, for instance, web-based Petri net teaching materials. Learning objects, created in this way, have their underlying semantics described in RDF form, and can be transformed into PNML as well as analysed with standard Petri net tools. P3 provides two kinds of RDF annotations (Handschuh *et al.*, 2003) for SVG:

- 1 As embedded meta-data – an RDF description is incorporated in SVG documents. The standard SVG has the `metadata` tag as an envelope for meta-data (Figure 15).
- 2 As remote meta-data – an RDF description is in a separated document.

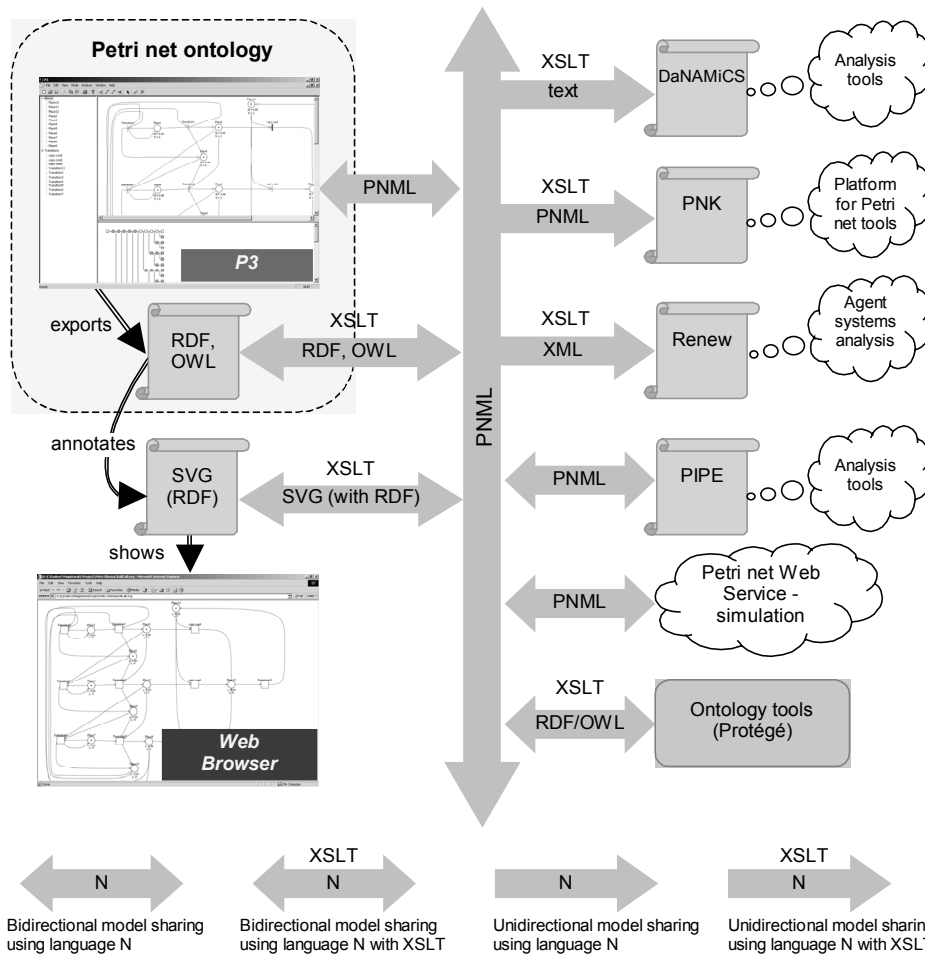
Figure 15 An example of an RDF-annotated SVG document that contains a simple Petri net (n1) consisting of a place (p1), a transition (t1), and an arc (a1) that connects p1 and t1

<pre><?xml version="1.0" encoding="ISO-8859-1"?> <svg width="2000px" height="2000px"> <metadata> <rdf:RDF> <!-- We omitted namespace definitions due to their length --> <Place rdf:about="p1" ID="p1" rdfs:label="p1"> <position rdf:resource="p1posGldesc"/> <initialMarking rdf:resource="p1initmarking"/> <marking rdf:resource="p1marking"/> <name rdf:resource="p1name"/> </Place> <Transition rdf:about="t1" ID="t1" rdfs:label="t1"> <position rdf:resource="t1posGldesc"/> <name rdf:resource="t1name"/> </Transition> <Arc rdf:about="a1" ID="a1" arcType="normal" rdfs:label="a1"> <fromNode rdf:resource="p1"/> <toNode rdf:resource="t1"/> <multiplicity rdf:resource="a1multi"/> </Arc> <!-- RDF descriptions for properties of Place, Transition, and Arc are omitted due to their length --> <Net rdf:about="n1" ID="n1" rdfs:label="n1"> <elements rdf:resource="p1"/> <elements rdf:resource="t1"/> <elements rdf:resource="a1"/> </Net> </rdf:RDF> </metadata></pre>	<pre><title>Petri net - SVG format</title> <desc>Exported from the P3 Petri net tool</desc> <g id="a1"> <path class="Line" d="M76 176 L 217 176"/> <g transform="translate(217 ,176)"> <g transform="translate(-22, 0)"> <g transform=" rotate(0)"> <path class="Line" d="M 0 -3 L 7 0"/> <path class="Line" d="M 7 0 L 0 3"/> </g> </g> </g> </g> <g id="p1"> <circle class="Place" r="15" cx="76" cy="176"/> <text class="Label" text-anchor="middle" x="76" y="160">p1</text> </g> <g id="t1"> <rect class="Transition" x="202" y="161" width="30" height="30"/> <text class="Label" text-anchor="middle" x="217" y="160">t1</text> </g> </svg></pre>
---	--

Although P3 uses RDF, it does not mean that we have abandoned PNML. On the contrary, since we implemented an XSLT (from RDF to PNML), we continued using PNML. Actually, we enhanced PNML because one can use P3 to convert a PNML model to RDF, and then the Petri net model can be validated against the Petri net ontology. That way, we achieved a semantic validation of Petri net models. Of course, PNML is very useful since it contains well-defined concepts for Petri net models interchange and it is

now used by many Petri net tools. Furthermore, since we implemented the XSLTs from PNML to Petri net formats of other Petri net tools, we can also employ their Petri net analysis capabilities (e.g., Petri net invariant analysis).

Figure 16 Petri net infrastructure for the Semantic Web (that uses ‘PNML-based bus’ for model sharing): the Petri net ontology, current Petri net tools, P3 tool, web-based applications, Petri net web service, and ontology tools for validation of Petri net documents using the ontology



In Figure 16, we show the Semantic Web infrastructure for Petri nets, which is now implemented. This infrastructure summarises all the major features of P3. The central part of this infrastructure is PNML, since it would be (probably) a part of the future High-level Petri net standard (Kindler, 2004). P3 can be linked with other Petri net tools through PNML (e.g., with PIPE), or by using additional XSLTs on PNML models (DaNAMiCS, Renew, and PNK). Also, P3 has XSLTs for conversions between PNML and RDF in both directions. Besides, P3 generates SVG by using XSLT from PNML to SVG. An XSLT is developed to generate the RDF-annotated SVG from the PNML. We

have also developed the XSLT that transforms RDF-annotated SVG documents to PNML. This XSLT is based on the XSLT from RDF to PNML. Hence we have XSLTs for conversions between PNML and SVG in both directions.

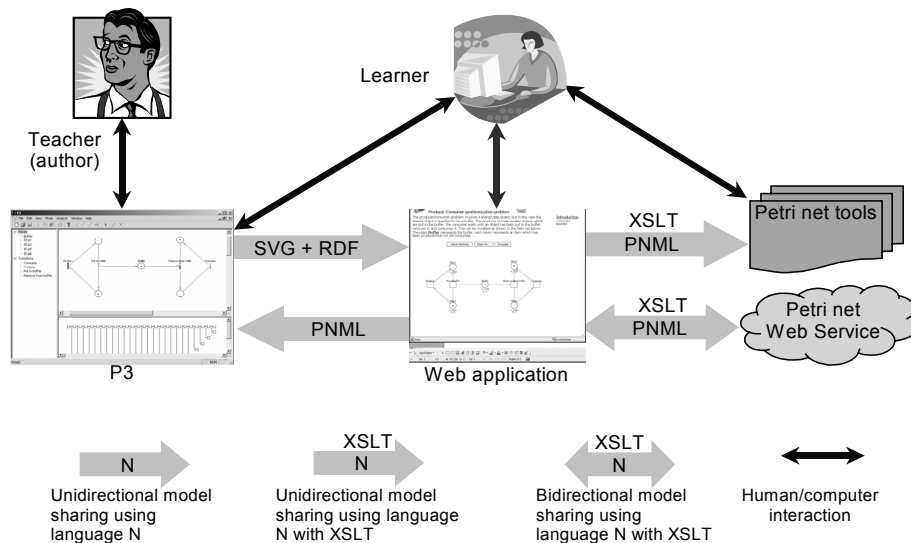
7 An application example

The previously presented Petri net infrastructure for Semantic Web can have various applications in practice. Here, we introduce a web-based educational system that uses Petri nets. This system was developed following proposed directions for the next generation of educational web systems in the context of Semantic Web.

Systems of this type have two kinds of users: teachers and students. A teacher creates learning materials using P3 tool. P3 has the capacity to save Petri net models in SVG format that can be annotated using RDF compliant to RDFS Petri net ontology. In this way, generated materials for learning Petri nets can be used in different web systems (e.g., one can develop a dynamic web learning application that uses Petri nets' SVG format to illustrate learning subject). Students use these materials for studying.

In order to empower web applications with the ability to perform interactive simulation of Petri net models, implementation of the logic of Petri net execution is needed. This can be achieved using web service for Petri net simulation presented in Havram *et al.* (2003). This is a PNML-based web service, *i.e.*, it uses PNML Petri net model as input, performs one simulation step and generates result, again, in PNML format. Web application should forward Petri net model to the web service. This model is converted from RDF-annotated SVG format into PNML format using an XSLT. Once the simulation is finished, another XSLT is used to transform the result from PNML to RDF-annotated SVG format. Both XSLTs are part of the proposed infrastructure. Web application should only implement calls to web service procedures; the whole logic of Petri net model simulation is implemented in web service. Figure 17 depicts a suggested approach to educational systems development using proposed Petri net infrastructure for the Semantic Web.

Figure 17 A proposed approach to using Petri net infrastructure for the Semantic Web in web-based educational systems



8 Conclusion

The main idea of this paper is that the Petri net ontology should provide the necessary Petri net infrastructure for the Semantic Web. The infrastructure understands Petri nets sharing using XML-based ontology languages (*i.e.*, RDFS and OWL). The Petri net ontology and Semantic Web languages do not abandon the PNML. On the contrary, we presented the ‘PNML-based bus’ that takes advantage of the PNML together with the Petri net ontology. That way, we can exploit the potentials of current Petri net tools in the context of the Semantic Web. We also presented P3, the Petri net tool that creates ontology-based Petri net models. Its abbreviated version, its technical description, as well as a few developed XSLTs can be downloaded from <http://www15.brinkster.com/p3net>.

The paper gives guidelines for putting Petri nets on the Semantic Web. It also shows complementary features of the Petri net syntax and semantics by the example of the PNML and the Petri net ontology. The example of RDF-based annotation of SVG documents indicates how to annotate other XML formats (*e.g.*, Web Service Description Language – WSDL). This opens the door to incorporating ‘Petri net-driven intelligence’ into web-based applications (*e.g.*, web service composition, web service analysis and simulation (Narayanan and McIlraith, 2003)).

In the future, the P3 tool will support OWL and OWL-based annotation of SVG documents with Petri net graphs. Furthermore, we will use this annotation principle to develop a Petri net web-based learning environment, as well as to create Learning Object Metadata (LOM) repositories of Petri net models.

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Note

- 1 <http://protege.stanford.edu/plugin/uml>